

# Beamforming

PETER ISHO

# What is Beamforming?

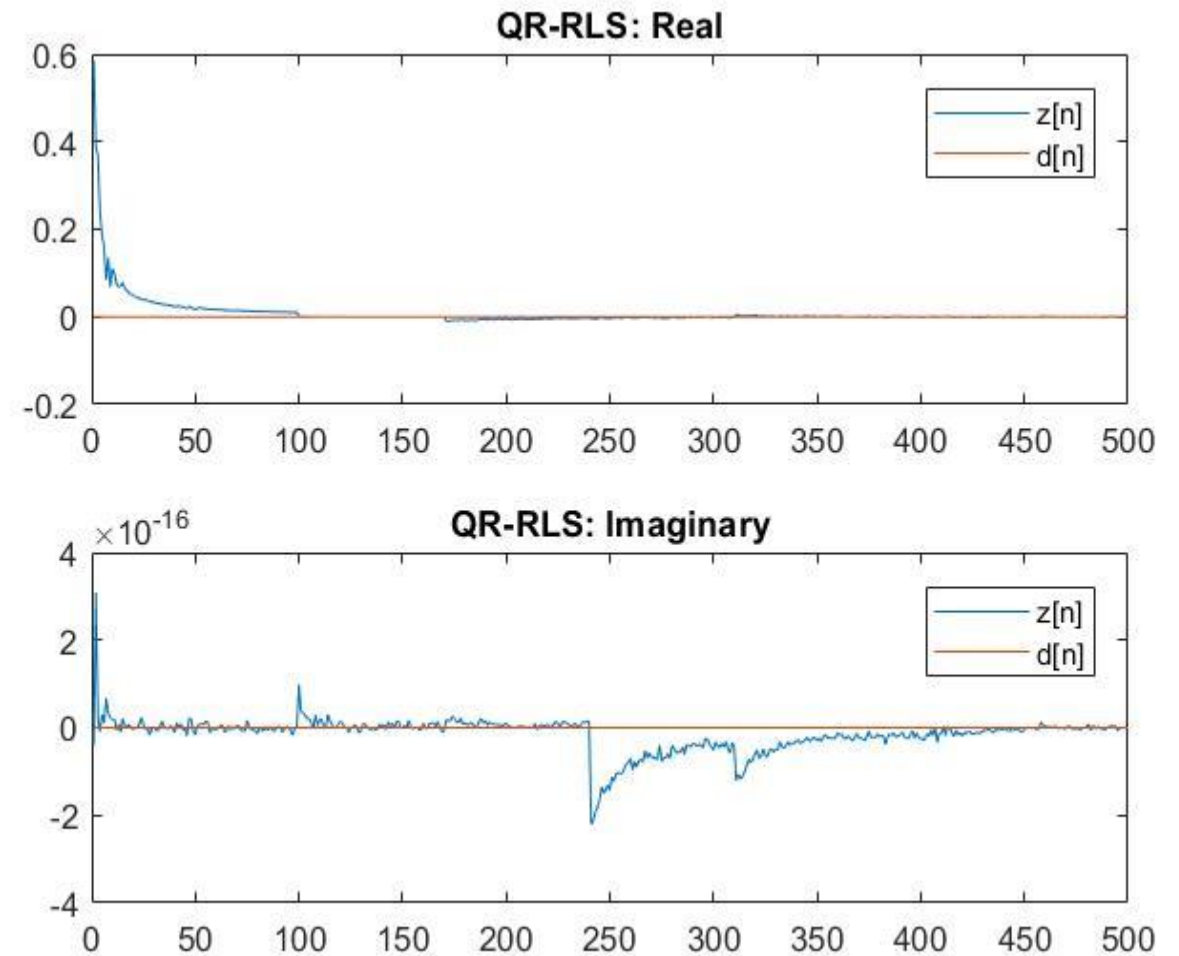
- ▶ Essentially a directed signal
- ▶ Signals output in all directions
- ▶ Faster, stronger, and more range

# Broad Overview

- ▶ Input matrix of  $M \times N$  data
- ▶  $M$  sensors outputting signals from all directions
- ▶ One output direction after beamformer

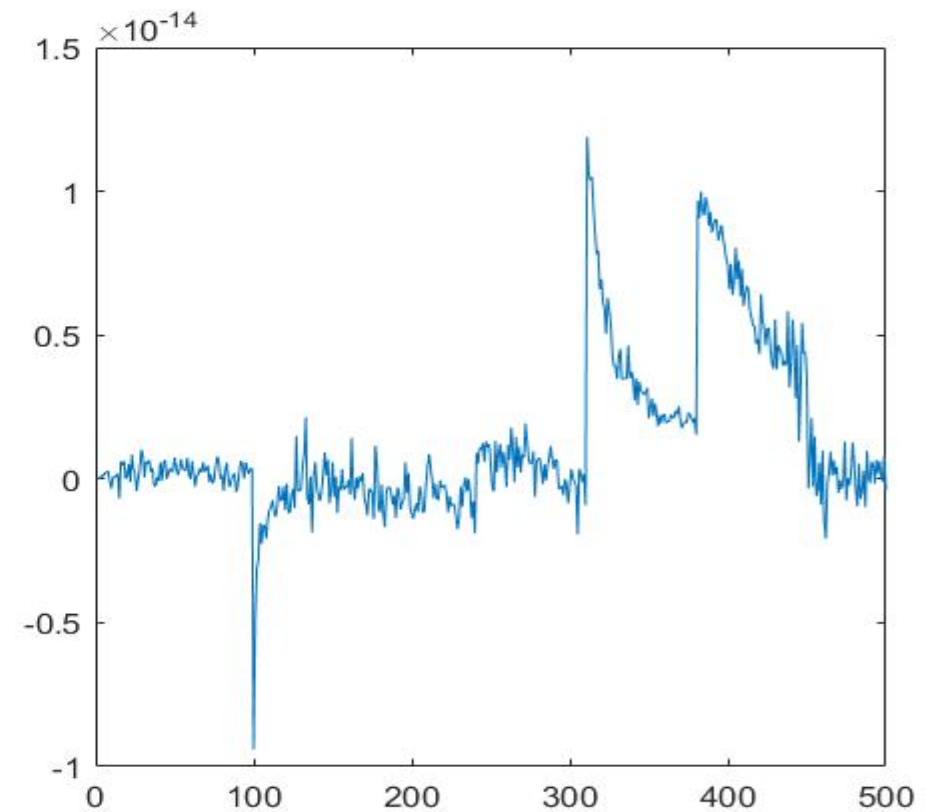
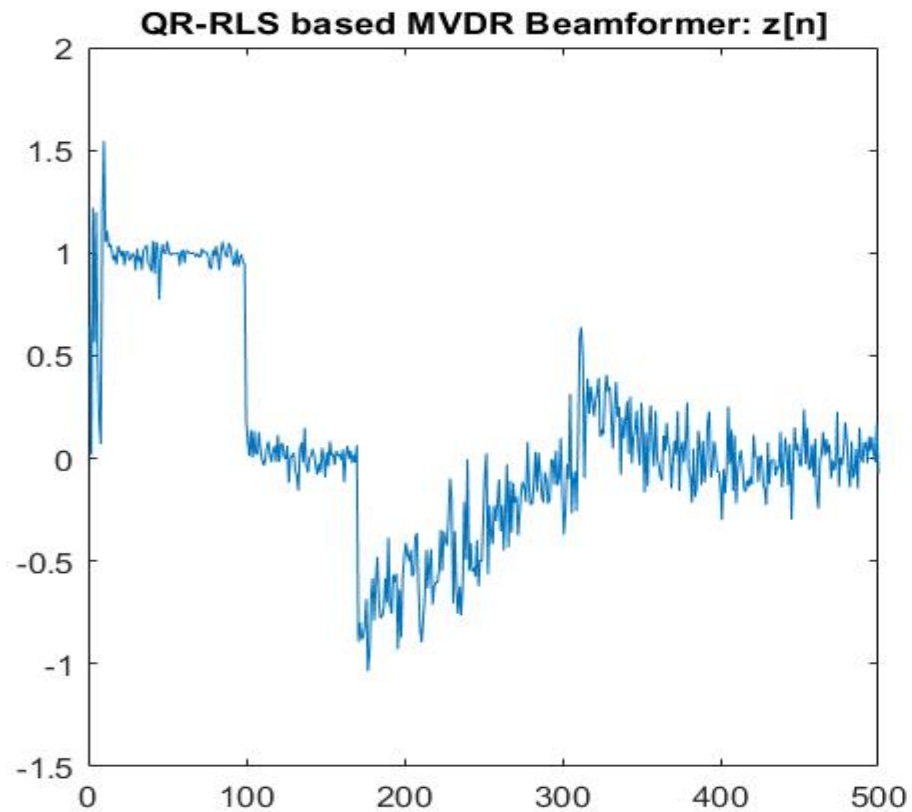
# QR-RLS Algorithm

- ▶ Professor Llamocca helped with a MATLAB implementation
- ▶ Left Side – Real
- ▶ Right Side – Imaginary
- ▶ Target is at zero so output strives for zero



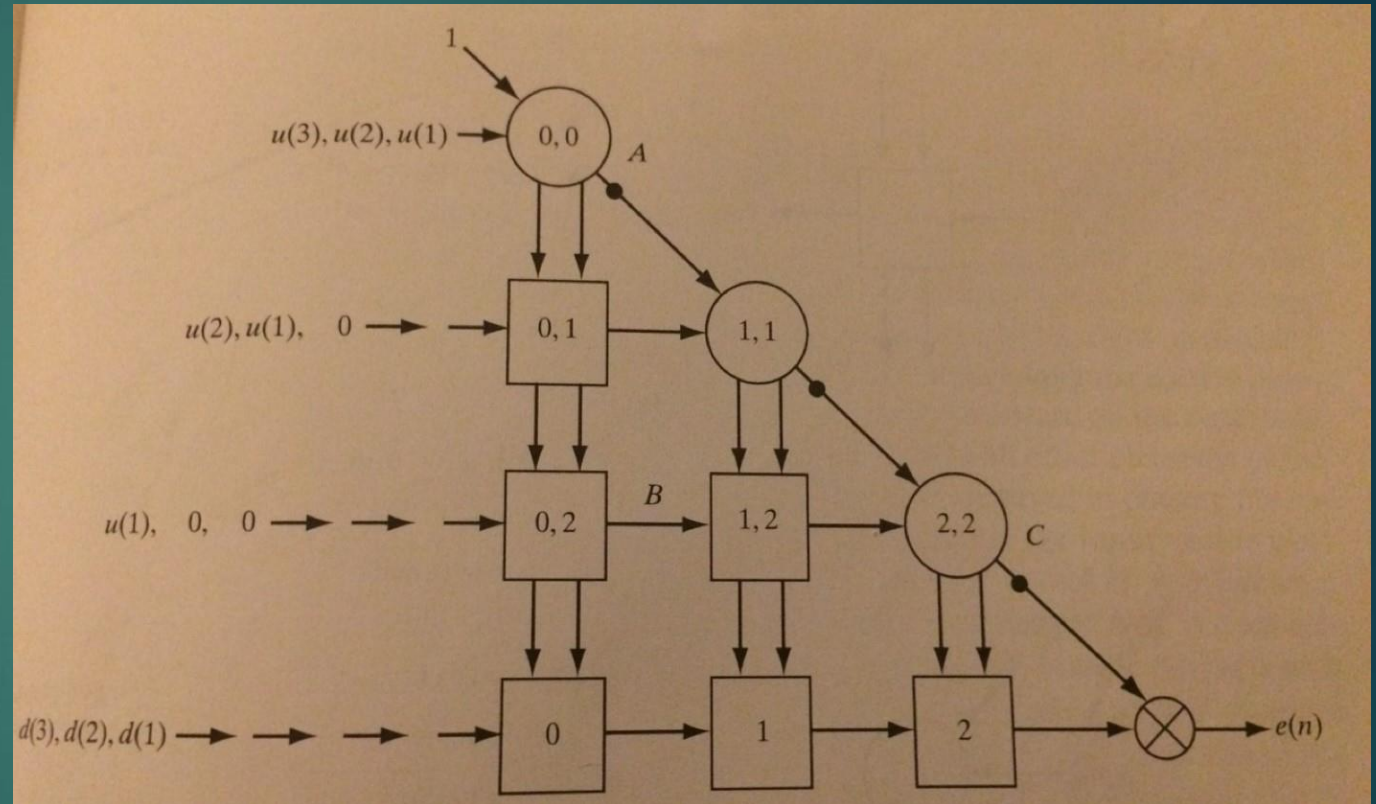
# Output Signal

- ▶ This is the output signal after the beamformer



# Hardware Implementation

- ▶ Systolic Array
- ▶ Initial Plan to design
- ▶ Timing would be hard



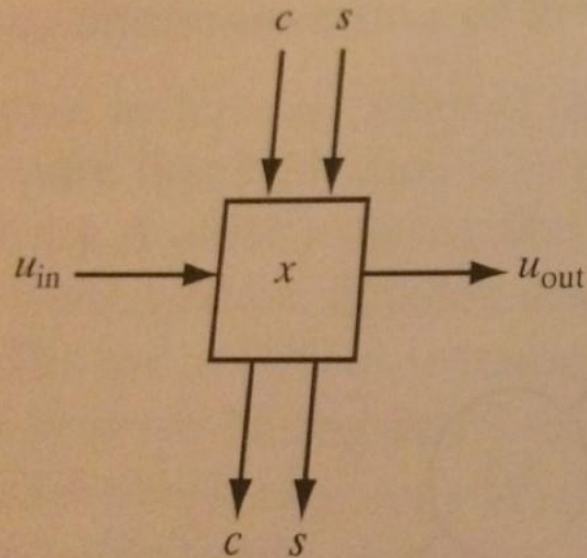
# Complex Numbers

- ▶ Some of these signals are complex
- ▶ Therefore, a real and imaginary path are used
- ▶ Input data =  $.56 + .85i$
- ▶ Split this into two signals: Real =  $.56$  and Imaginary =  $.85$



# Internal Cell

- Two multiplications and two additions



$$\begin{aligned} \checkmark u_{out} &\leftarrow cu_{in} - s^* \lambda^{1/2} x \\ \checkmark x &\leftarrow su_{in} + c \lambda^{1/2} x \end{aligned}$$

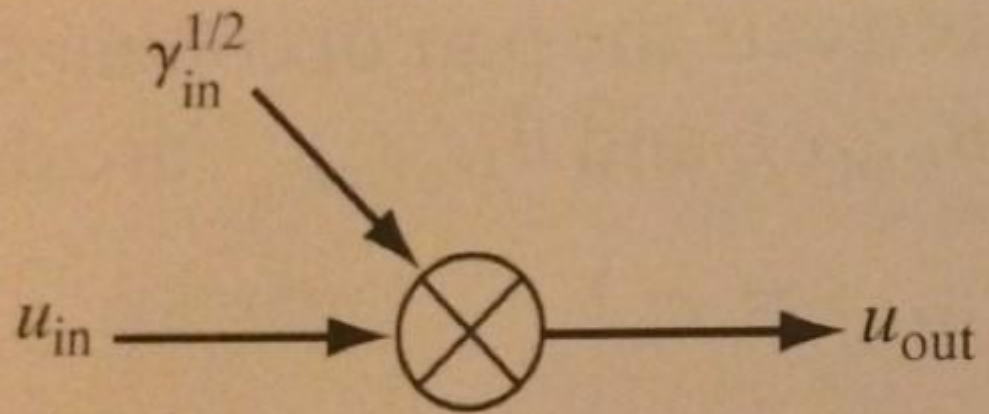
Initialization:  
At  $n = 0$ , set  
 $x = 0$   
 $c = 1$   
 $s = 0$

(a)



# Final Processing Cell

- ▶ One multiplication for the output of the beamformer

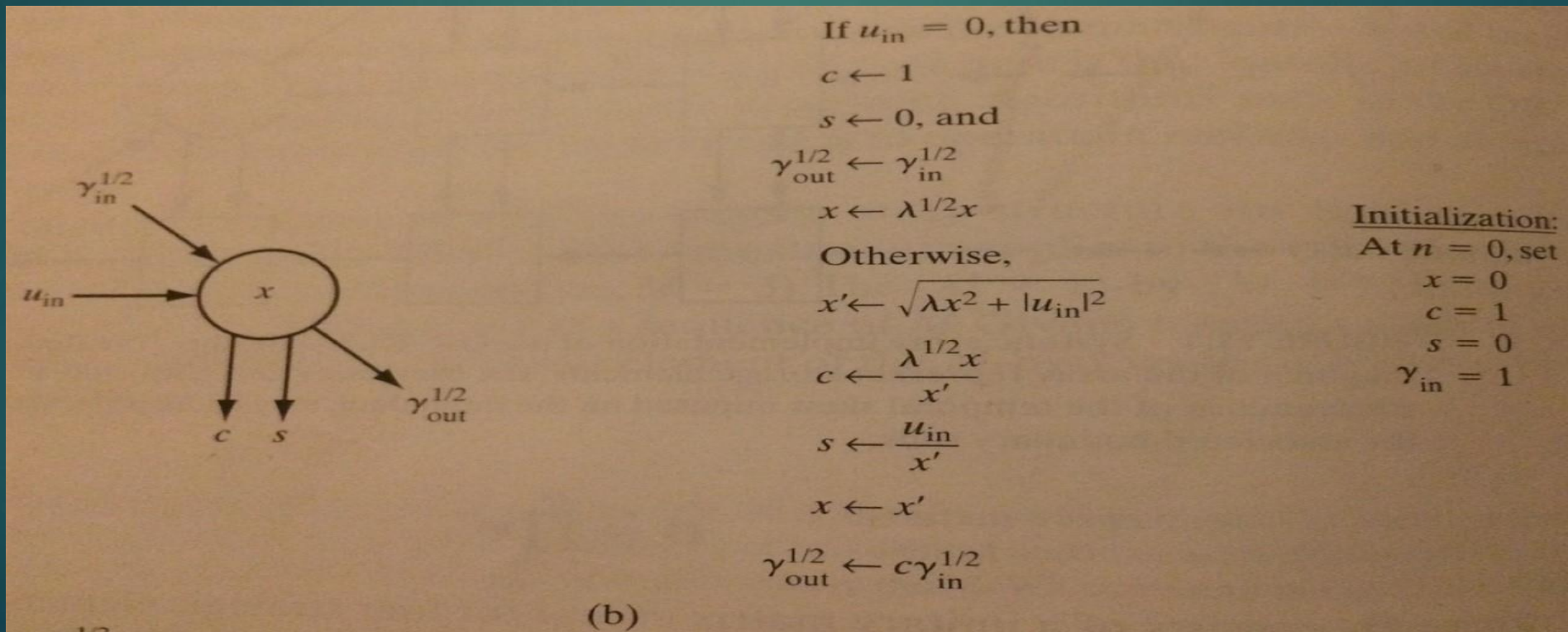


$$u_{out} \leftarrow \gamma_{in}^{1/2} u_{in}$$

(c)

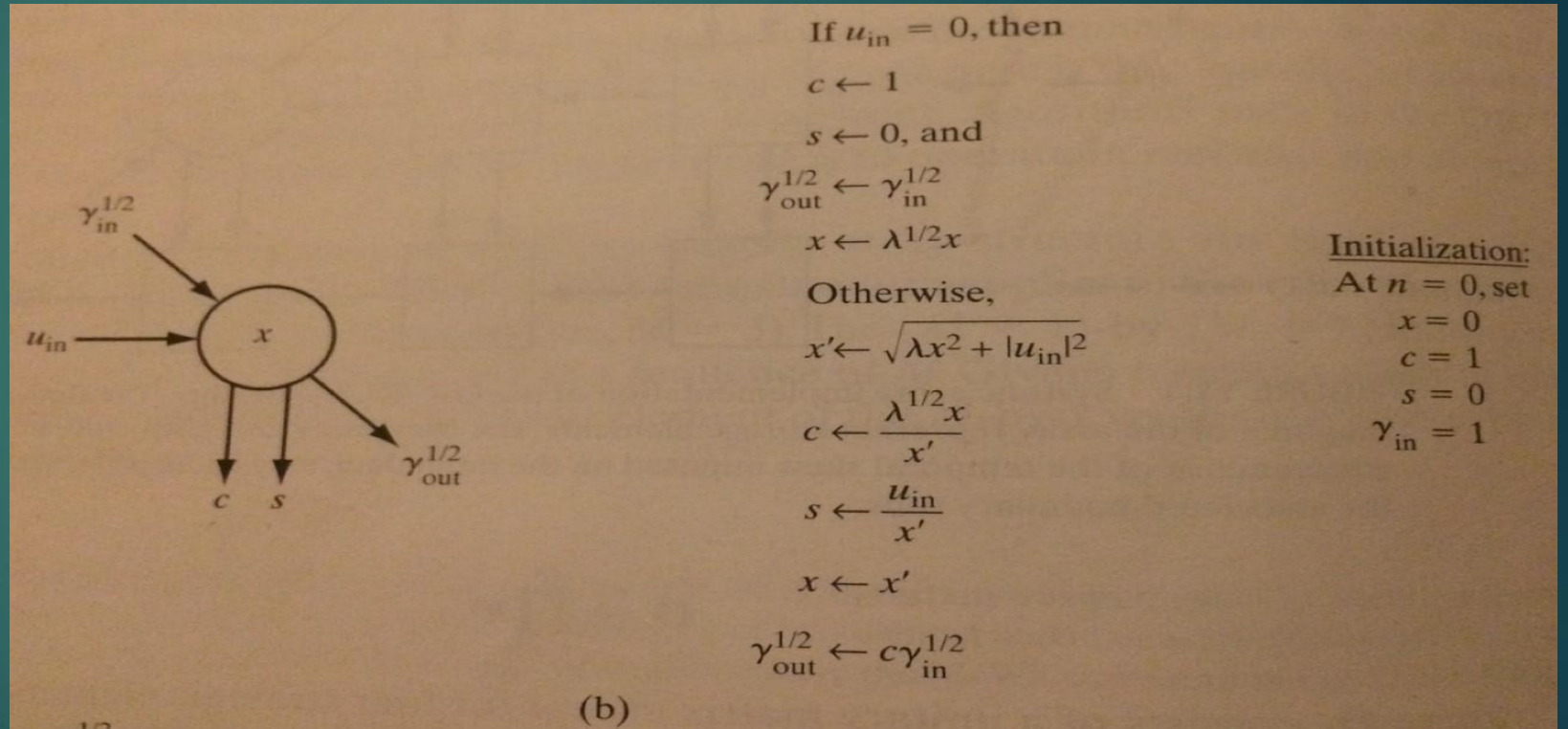
# Edge Cell

- ▶ Contains Cordic, Division, Multiplication
- ▶ Entire thing Pipelined
- ▶ Right now I have the non-pipelined version complete



# “FSM”

1. Calculate  $\text{abs}U$
2. Calculate  $x'$
3. Calculate  $cO$ ,  $sO$ ,  $x$
4. Calculate  $yO$



# Accuracy – Non-Pipelined

Inputs	Outputs Vivado	Outputs MATLAB
Y_in = 1.0	X = .309997	X = 0.3101
U = 1.28 + .2824i	C = 0.0	C = 0.0
X = 0.0	S = .41284 + .91119i	S = 0.4127 + 0.9109i
	Y = 0.0	Y = 0.0

# Accuracy – Non-Pipelined

Inputs	Outputs Vivado	Outputs MATLAB
Y_in = 1.0	X = 0.328247	X = 0.3283
U = -0.03564 – 0.10211i	C = 0.944396	C = 0.9442
X = 0.309997	S = -0.10858 – 0.31103i	S = -0.1084 – 0.311i
	Y = 0.944396	Y = 0.9442



# Accuracy – Non-Pipelined

Inputs	Outputs Vivado	Outputs MATLAB
Y_in = 0.6854	X = 0.34505	X = 0.9246
U = 0.2304 – 0.833i	C = 0.95556	C = 0.3552
X = 0.328247	S = 0.6707 + 1.575i	S = 0.2492 – 0.901i
	Y = 0.65496	Y = 0.2435

- Due to CORDIC [16 14] FX format
- The real value can't be expressed due to limited number of integer bits

# Can't Pipeline Feedback Loop

CORDIC								
> Xin[15:0]	0.127990	0.0	0	-00				
> Yin[15:0]	0.282470	0.0	0	-00				
> Zin[15:0]	0.0							
> Xout[15:0]	0.0			0.0			0.0	
> Yout[15:0]	0.0			0.0			-00	
> Zout[15:0]	0.0	0.0	0	0	0	0	0	0
> E[0:0]	1	0	1	0	1			
> v[0:0]	0		0				1	0



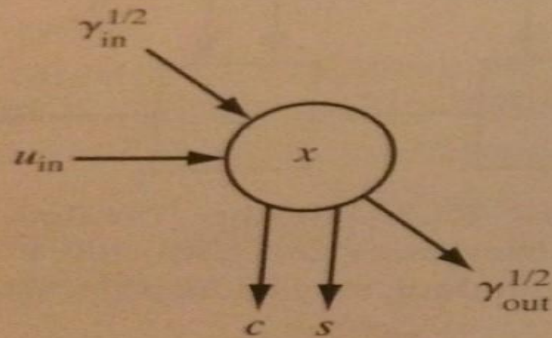
# Cycle Time

- ▶ Theoretically takes 1 cycles
  - ▶ Actually takes 152 cycles PER boundary cell
    - ▶ CORDIC
      - ▶ CORDIC
        - ▶ 2 parallel divisions
          - ▶ 1 multiplication
- ▶ Can't Pipeline because of feedback loop
  - ▶ This makes it pointless to pipeline anything else
  - ▶ This is the cause of the increased cycle time

# X outgrows [16 14]

- ▶ Theoretically takes 1 cycle
  - ▶ Actually takes 152 cycles

Iterations	x	Integer Bits
100	8.53	4
1000	25.32	5
10000	81,98	7

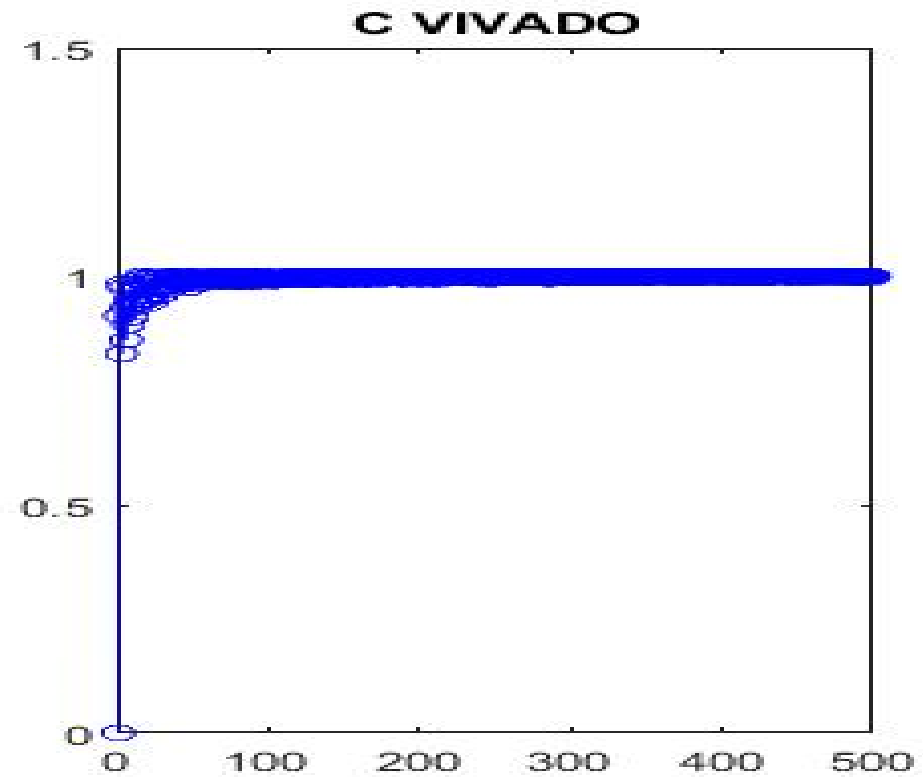
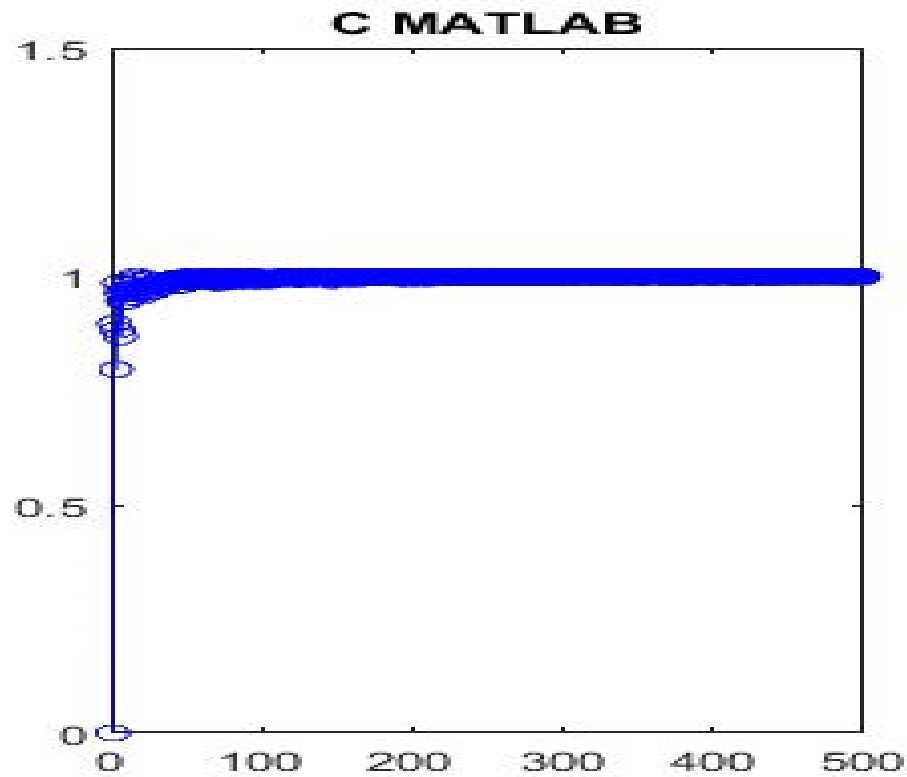


If  $u_{in} = 0$ , then  
 $c \leftarrow 1$   
 $s \leftarrow 0$ , and  
 $\gamma_{out}^{1/2} \leftarrow \gamma_{in}^{1/2}$   
 $x \leftarrow \lambda^{1/2}x$   
Otherwise,  
 $x' \leftarrow \sqrt{\lambda x^2 + |u_{in}|^2}$   
 $c \leftarrow \frac{\lambda^{1/2}x}{x'}$   
 $s \leftarrow \frac{u_{in}}{x'}$   
 $x \leftarrow x'$   
 $\gamma_{out}^{1/2} \leftarrow c\gamma_{in}^{1/2}$

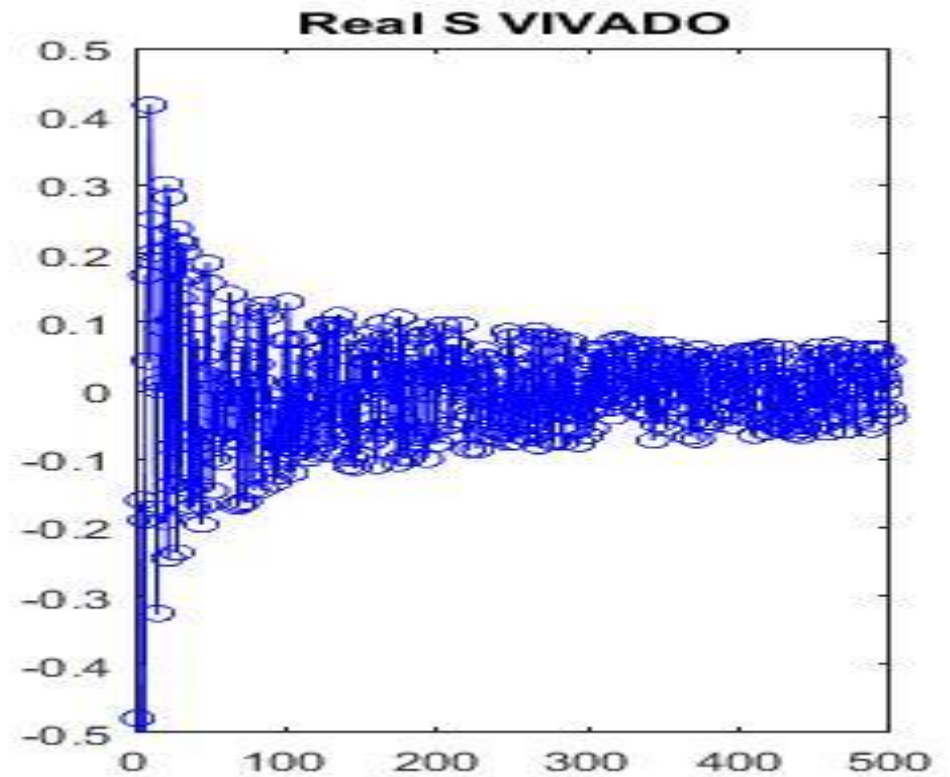
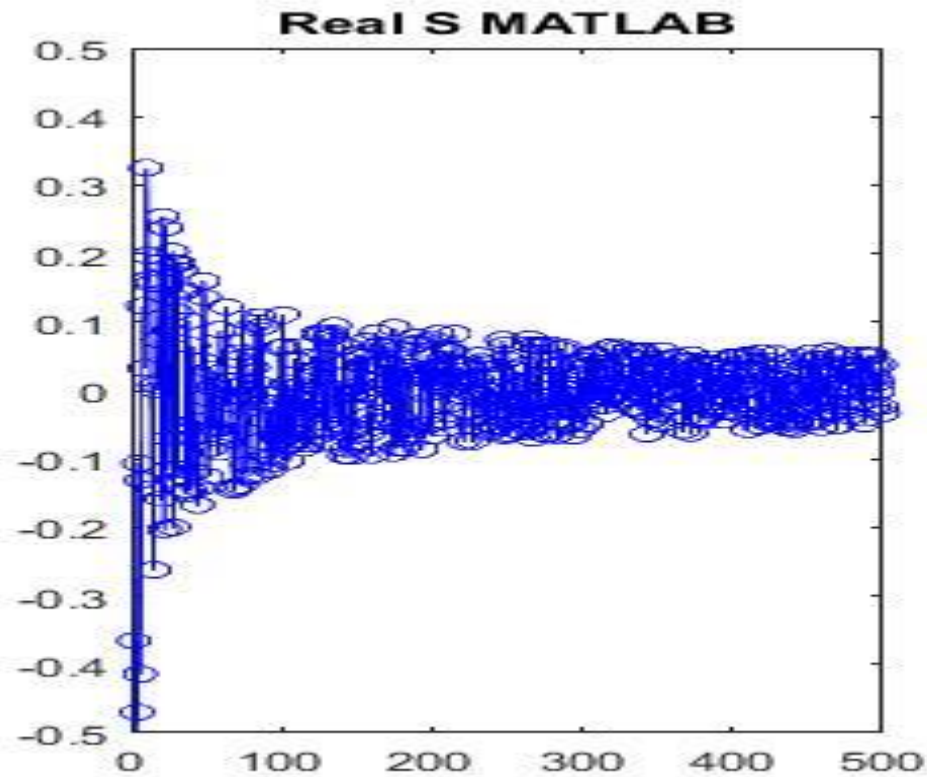
**Initialization:**  
At  $n = 0$ , set  
 $x = 0$   
 $c = 1$   
 $s = 0$   
 $\gamma_{in} = 1$

(b)

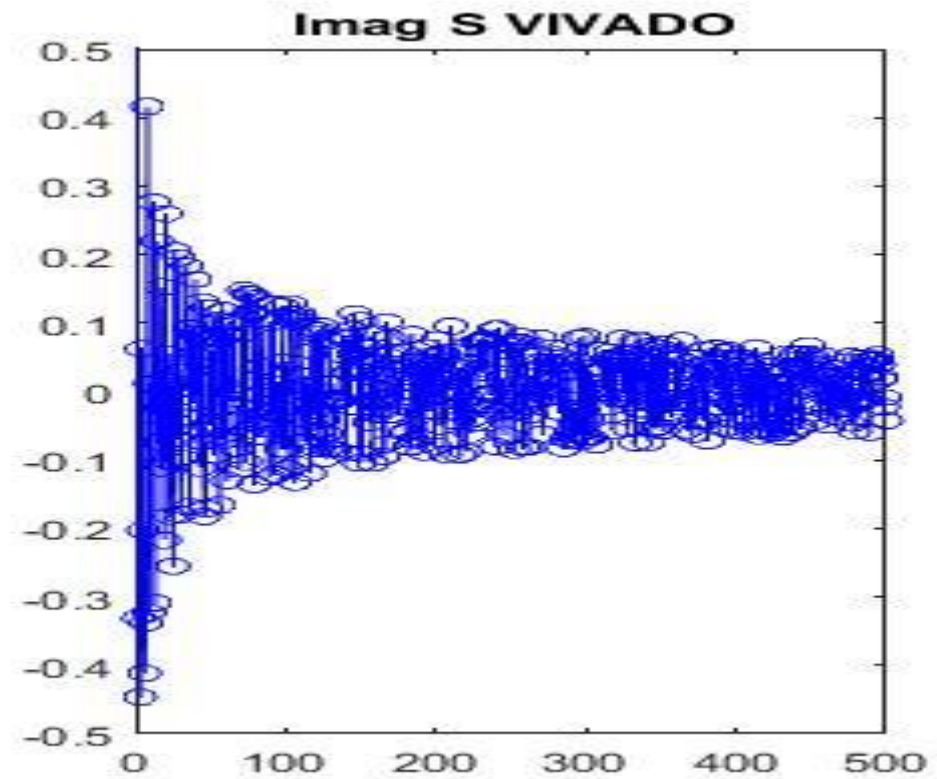
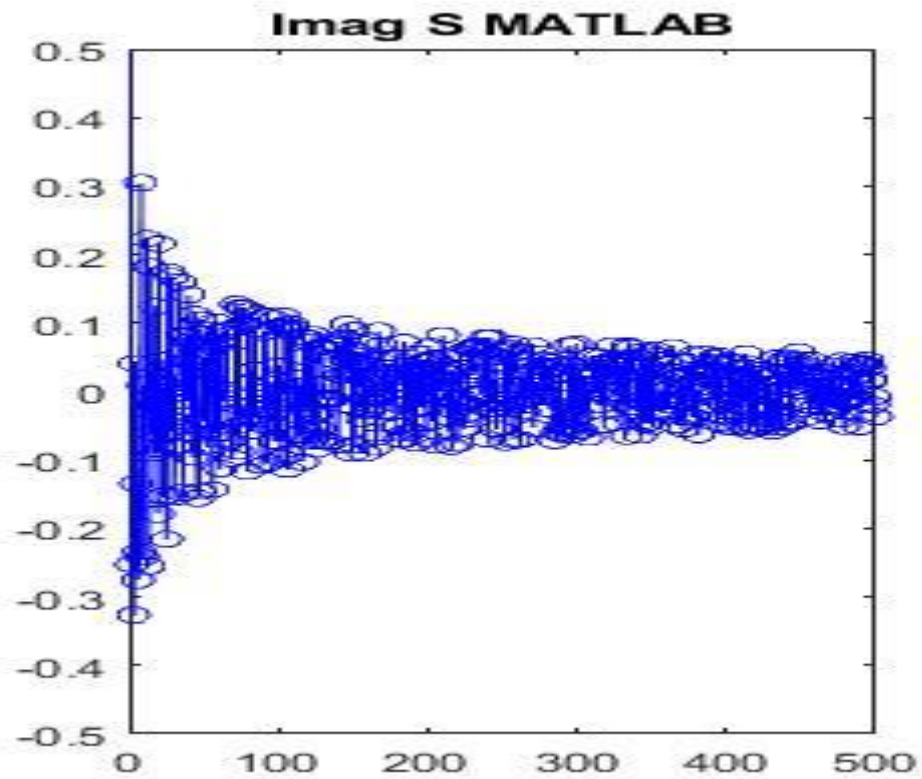
# Simulation - 500 Inputs



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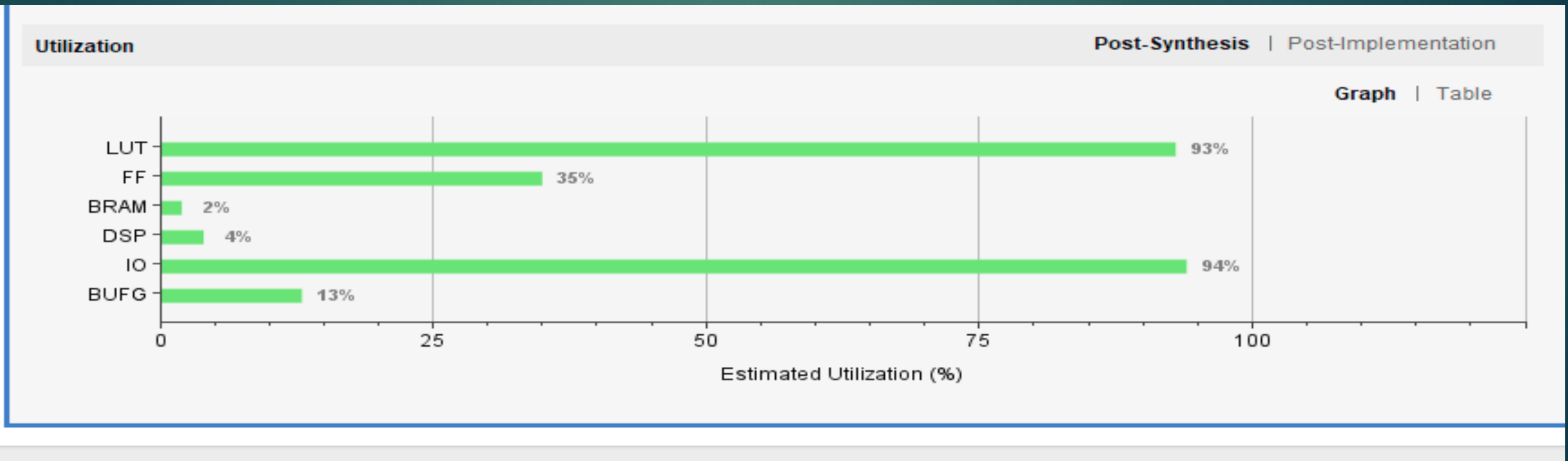


# Simulation - 500 Inputs



# 3 Antennas

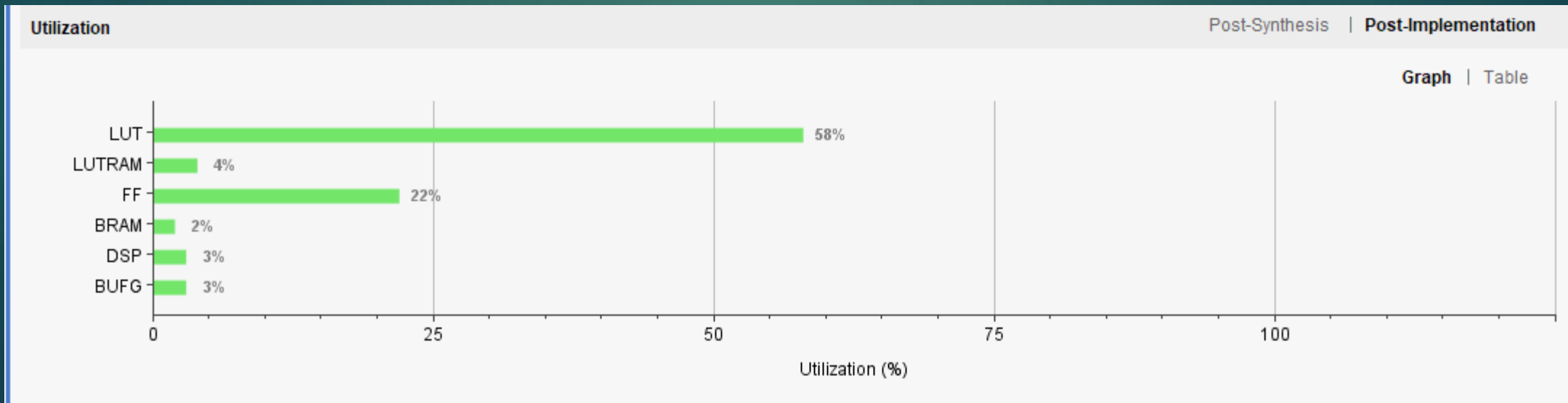
- ▶ Surpassed the number of LUTs on the FPGA
- ▶ 93% only my hardware
- ▶ Had to move down to 2 antennas





# 2 Antennas

- ▶ Successfully used AXI-Full with 2 antenna beamformer
- ▶ Didn't have time to analyze results
- ▶ Pretty sure they were incorrect
- ▶ No demo for the 2 antenna beamformer





# AXI-Full Interface

- ▶ Using iFIFO and oFIFO as before
- ▶ Develop FSM
- ▶ Write data on iFIFO one after another
- ▶ Write data from oFIFO when v signal is high

# Future Development

- ▶ Estimation?
- ▶ Have a working Beamformer
- ▶ Eventually hook an antenna up to fpga and test

# Questions?

